

# Estimating Sea Lion Abundance from Aerial Surveys and Capture-Recapture Data

A work in progress

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NOAA Fisheries  
Protected Species Assessment Workshop II  
February 12, 2019



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# How can we estimate Steller sea lion abundance?

## Some history

- Calkins & Pitcher (1982) reconstruct age distribution to estimate total abundance
- Ratio pups : total = 4.5
- pup counts  $\times$  4.5 used ever since

# What data to we have / can we get?

## Capture-recapture



- Only mark pups
- Abundance estimation requires marking adults

# What data to we have / can we get?

## Areal surveys



- Pups counts reliable
- Nonpups are tricky [foraging or not present]

# Overall goal

Want:

- $N$  = Total number of wDPS sea lions in 2018
- Other abundance items, e.g.,  $N_f$  = Total number of adult (4+) females

Have data:

- **C** = capture histories of pups marked since 2000
- **P** = pup counts at rookeries since 1986 (and before)

# A Bayesian posterior predictive approach

Q: What do we know about nonpups?

A: They were once pups!

Notation (separate for each sex)

- $P_y$  = number of pups observed in year  $y$
- $N_{a,y}$  = Abundance of age  $a$ , individuals year  $y$
- $S(t|s)$  = Survivorship to age  $t$  given alive at age  $s$

Age-structured model

- $[N_{a,y} | P_{y-a}, S(\cdot|\cdot)] = \text{Binom}(P_{y-a}, S(a|0))$
- Note, no need for natality components!

# Posterior distribution

Abundance

$$[\mathbf{N}_{2018} | \mathbf{P}, \boldsymbol{\theta}] = \prod_{a=1}^{30} \text{Binom}(N_{a,2018} | P_{2018-a}, S_{\boldsymbol{\theta}}(a|0))$$

Survival

$$[\boldsymbol{\theta} | \mathbf{C}] \propto \text{CJS}(\mathbf{C} | \boldsymbol{\theta}) \cdot [\boldsymbol{\theta}]$$

Bayesian predictive distribution

$$[\mathbf{N}_{2018} | \mathbf{P}, \mathbf{C}] = \int [\mathbf{N}_{2018} | \mathbf{P}, \boldsymbol{\theta}] \cdot [\boldsymbol{\theta} | \mathbf{C}] d\boldsymbol{\theta}$$

# Ages-specific survival modeling



# Survival analysis

## Hazard function

$h(t)$ , describes probability of death in a short age span, i.e.,  
 $P(\text{death} \in (t, t + \delta]) \approx h(t) \times \delta$   
where  $\delta \rightarrow 0$

## Survival function

Probability of survival to age  $t$  given alive at age  $s$ :

$$\begin{aligned} S(t|s) &= \exp \left\{ - \int_s^t h(u) du \right\} \\ &= \exp \{ -H(s, t) \} \end{aligned}$$

# Modeling hazard rate for Steller sea lions

$$h(t) = \alpha h_{juv}(t) + \eta h_{ad}(t) + \gamma$$

- $\alpha, \eta, \gamma$  are  $> 0$ .
- $h_{juv}(t)$  is a Weibull CDF
- $h_{ad}(t)$  increases exponentially
- $\gamma$  is the baseline hazard

# CJS Modeling

4 regions; 8 sites

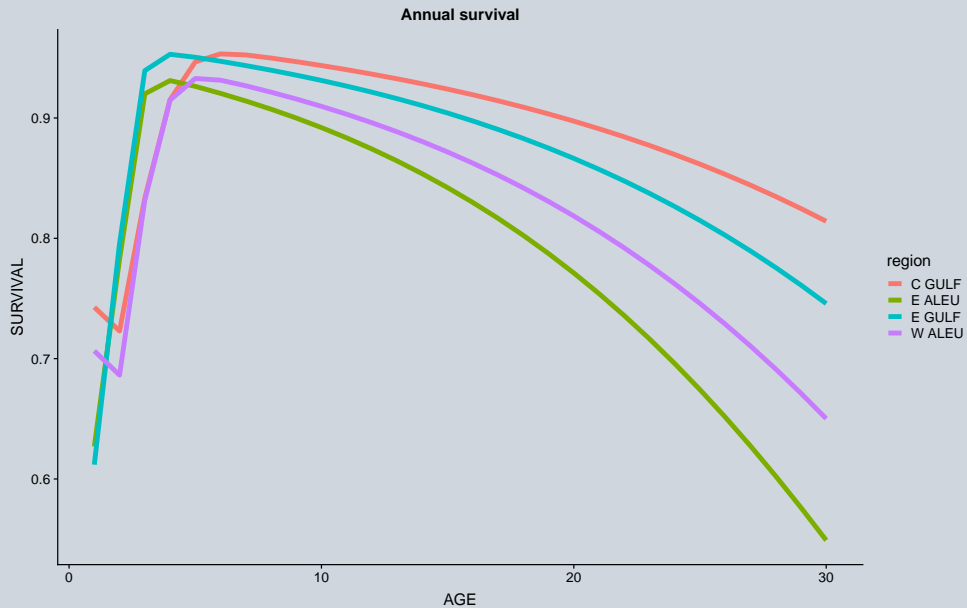
Survival parameters

- overall mean
- normal random effects for region
- variance components have exponential prior to induce sparsity

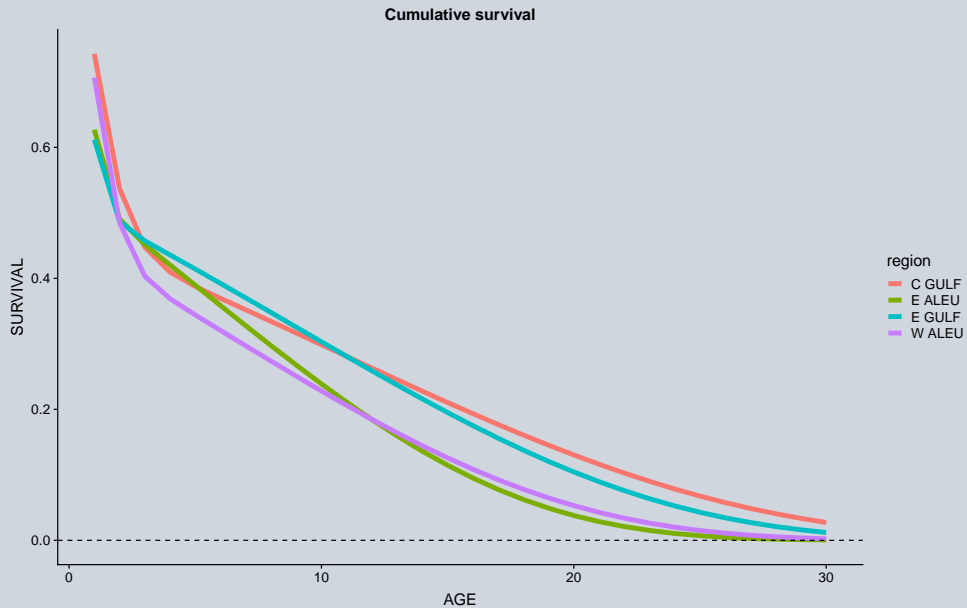
Detection parameters

- regional intercept
- site specific random effect
- site  $\times$  occasion random effects
- exponential variance components

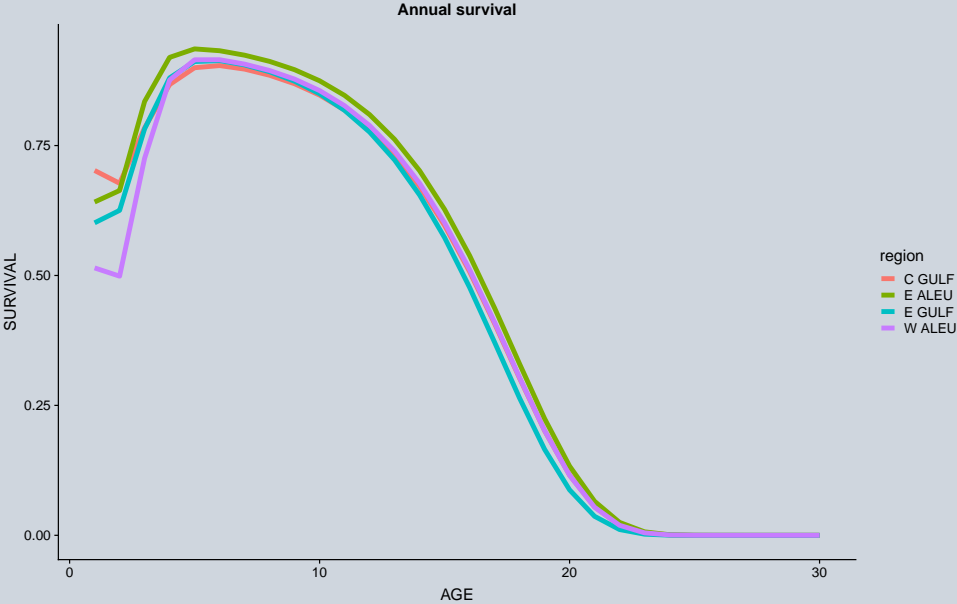
# Survival results Female



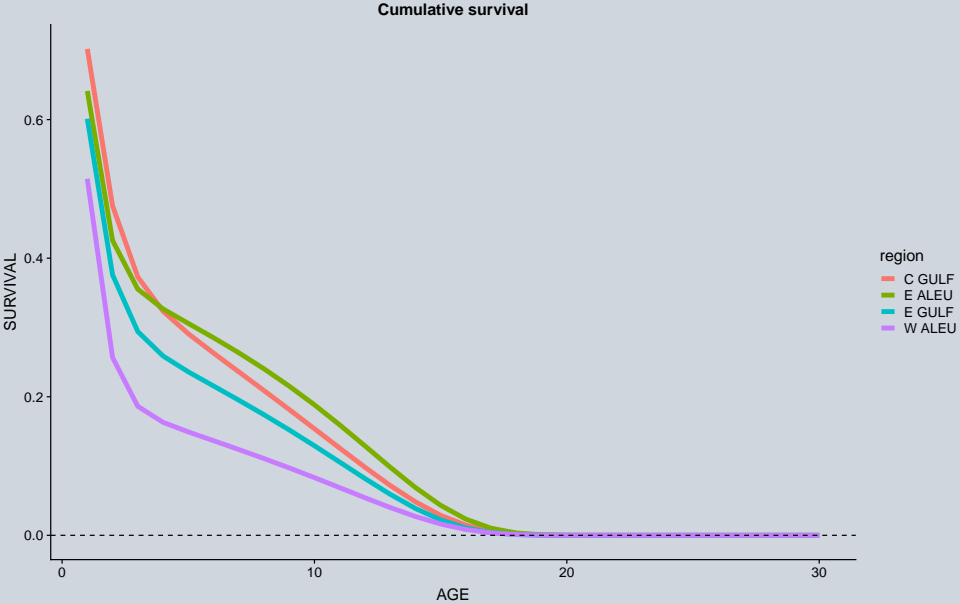
# Survival results: Female



# Survival results: Male



# Survival results: Male



To do:

A pragmatic approach for  
abundance



# Monte Carlo prediction of $N_{a,y}$

- ① Fit CJS model to survival data and obtain MAP,  $\hat{\theta}$ , and sample covariance,  $\hat{\Sigma}$
- ② Approximate  $[\theta|\mathbf{C}] \approx N(\theta|\hat{\theta}, \hat{\Sigma})$
- ③ For  $r$  in 1 to many
  - ① Sample  $\theta^{(r)} \sim N(\theta|\hat{\theta}, \hat{\Sigma})$
  - ② Sample  $\mathbf{P}^{(r)}$  using agTrend analysis
  - ③ Sample  $\mathbf{N}_y^{(r)} \sim [\mathbf{N}_y|\mathbf{P}, \theta^{(r)}]$
  - ④ Summarize quantity of interest, e.g., total abundance,  
$$N_{2018}^{(r)} = \sum_{a=0}^{30} N_{a,2018}^{(r)}$$

# An earlier attempt

64,029 [61,093–66,943]

